

## Alternating Current

### Summary

In **AC** the Voltage (and Current) oscillate up and down in SHM.

$$V = V_{\max} \sin(\omega t) \quad \omega \text{ is angular frequency of the supply (rad s}^{-1}\text{)}$$

where  $\omega = 2\pi f$   $f$  is the frequency of the supply (Hz)

To convert **AC** to **DC** it must be **rectified**. Diodes are commonly used because they conduct only in one direction.

Single diode: Half wave rectifier

Rectifier bridge (4 diodes): Full wave rectifier.

Ripples can be smoothed by large capacitor across the output.

**RMS Voltage** is defined as the **DC** voltage which produces the same power as **AC** with a peak voltage

$$V_{\text{peak}} = \sqrt{2} \times V_{\text{RMS}}. \text{ Similarly for Current: } I_{\text{peak}} = \sqrt{2} \times I_{\text{RMS}}$$

In an **AC** circuit:

Voltage and Current across a **Resistor** are in phase

Voltage across a **Capacitor** lags Resistor Voltage (and Current) by 90 degrees

Voltage across an **Inductor** leads Resistor Voltage (and Current) by 90 degr.

**Reactance** of a Capacitor and an Inductor are dependent on frequency:

**Capacitor:**  $X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C}$  easily conducts **high** frequency (small reactance)

**Inductor:**  $X_L = \omega L = 2\pi f L$  easily conducts **low** frequency (small reactance)

**AC filter** in audio electronics uses these properties

(Tweeter across Inductor; Woofer across Capacitor)

**Phasor diagrams** to illustrate Voltages and Reactance's:

**Supply Voltage** is **vector sum** of voltages across components

**Circuit Impedance** is **vector sum** of Reactance's of components

In RLC-circuit this means addition of three vectors.

Resonance Frequency when reactance of capacitor is equal the reactance of inductor:

$$X_C = \frac{1}{\omega C} = \omega L = X_L \text{ or } \omega = \frac{1}{\sqrt{LC}}.$$

Then Impedance = resistance of resistor.

Hence current is maximum.

This principle is used in a radio receiver, metal detector, etc.

